

Wybrane pary transformat (całkowych) Fouriera

No.	Sygnał $x(t)$	Widmo $X(\omega)$
1	$e^{-at}u(t)$	$\frac{1}{a + j\omega}$
2	$te^{-at}u(t)$	$\left(\frac{1}{a + j\omega}\right)^2$
3	$r_T(t) = \begin{cases} 1, & t < T/2 \\ 0, & t > T/2 \end{cases}$	$T \operatorname{sinc} \frac{\omega T}{2}$
4	$\Delta_T(t) = \begin{cases} 1 - \frac{ t }{T}, & t < T/2 \\ 0, & t > T/2 \end{cases}$	$T \operatorname{sinc}^2 \frac{\omega T}{2}$
5	$e^{-a t }$	$\frac{2a}{a^2 + \omega^2}$
6	$e^{-at}(\sin \omega_0 t)u(t)$	$\frac{\omega_0}{(a + j\omega)^2 + \omega_0^2}$
7	$e^{-at}(\cos \omega_0 t)u(t)$	$\frac{a + j\omega}{(a + j\omega)^2 + \omega_0^2}$
8	e^{-at^2}	$\left(\frac{\pi}{a}\right)^2 e^{-\omega^2/4a}$
9	$\operatorname{sinc} \frac{Tt}{2}$	$\frac{2\pi}{T} r_T(\omega)$
10	$\operatorname{sinc}^2 \frac{Tt}{2}$	$\frac{2\pi}{T} \Delta_T(\omega)$

Wybrane pary transformat Fouriera – ciąg dalszy

No.	Sygnał $x(t)$	Widmo $X(\omega)$
11	$\frac{1}{a^2 + t^2}$	$\frac{\pi}{a} e^{-a \omega }$
12	$\delta(t)$	1
13	1	$2\pi\delta(\omega)$
14	$u(t)$	$\pi\delta(\omega) + \frac{1}{j\omega}$
15	$e^{j\omega_0 t} = \cos \omega_0 t + j \sin \omega_0 t$	$2\pi\delta(\omega - \omega_0)$
16	$\cos \omega_0 t = \frac{e^{j\omega_0 t} + e^{-j\omega_0 t}}{2}$	$\pi[\delta(\omega - \omega_0) + \delta(\omega + \omega_0)]$
17	$\sin \omega_0 t = \frac{e^{j\omega_0 t} - e^{-j\omega_0 t}}{2j}$	$j\pi[\delta(\omega - \omega_0) - \delta(\omega + \omega_0)]$
18	sign t	$\frac{2}{j\omega}$
19	$(\cos \omega_0 t)u(t)$	$\frac{\pi}{2}[\delta(\omega - \omega_0) + \delta(\omega + \omega_0)] + \frac{j\omega}{\omega_0^2 - \omega^2}$
20	$(\sin \omega_0 t)u(t)$	$\frac{\pi}{2j}[\delta(\omega - \omega_0) - \delta(\omega + \omega_0)] + \frac{\omega_0}{\omega_0^2 - \omega^2}$

$$\delta(t) \triangleq \begin{cases} \infty, & t = 0 \\ 0, & t \neq 0 \end{cases}, \quad \int_{-\infty}^{\infty} \delta(t) dt = 1$$

$$1. \quad x(t)\delta(t - t_0) = x(t_0)\delta(t - t_0), \quad x(t)\delta(t) = x(0)\delta(t)$$

$$2. \quad \int_{-\infty}^{\infty} x(t)\delta(t - t_0) dt = x(t_0)$$

$$\text{Jeżeli } x(t) \equiv 0, \quad t < 0 \quad \text{to} \quad F\{x(t)\} = L\{x(t)\} \Big|_{s=j\omega}.$$